

# Modeling and analysis of surface roughness effects on sputtering, reflection and sputtered particle transport <sup>\*</sup>

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The microstructure of the redeposited surface in tokamaks may affect sputtering and reflection properties and subsequent particle transport. This subject has been studied numerically using coupled models/codes for near-surface plasma particle kinetic transport (WBC code) and rough surface sputtering (fractal-TRIM). The coupled codes provide an overall Monte Carlo calculation of the sputtering cascade resulting from an initial flux of hydrogen ions. Beryllium, carbon, and tungsten surfaces are analyzed for typical high recycling, oblique magnetic field, divertor conditions. Significant variations in computed sputtering rates are found with surface roughness. Beryllium exhibits high D–T and self-sputtering coefficients for the plasma regime studied ( $T_e = 30\text{--}75$  eV). Carbon and tungsten sputtering is significantly lower.

## 1. Introduction

Fusion surface erosion may depend on surface microstructure via changes in sputtered particle velocity distributions and by overall sputtering coefficients. This may be particularly true for a high redeposition plasma regime where near-surface impurity transport is important. A recent study examined sputtered impurity transport for high recycle, oblique magnetic field, tokamak divertor conditions [1]. The study used the WBC Monte Carlo code to compute the sub-gyro orbit motion of the particles in a fixed background D–T plasma. This work focused on modeling of plasma-impurity interactions, and treated the surface sputtering using analytical models appropriate for smooth surfaces. In the area of surface modeling, recent work has been done on modeling sputtering from rough surfaces by using fractal geometry in the TRIM binary collision code [2–3]. For this paper these codes, WBC and FTRIM, have been coupled to provide a more self-consistent calculation of the effects of microstructure on sputtering and transport, for typical high recycle divertor conditions. General goals of this work are to check on previous (favorable) self-sputtering results for

tungsten [1] and to provide estimates of D–T and self-sputtering coefficients for beryllium and carbon, for high recycling divertor conditions.

## 2. Computational model

Fig. 1 shows the model geometry. The (net) magnetic field lies in the  $z$ – $y$  plane and is uniform in the  $x$ -direction. The plasma has a uniform temperature,  $T_e = T_i$ , sound speed flow (prior to the sheath), and electron density prior to the sheath  $N_e = N_{e_0}$ . The sheath poten-

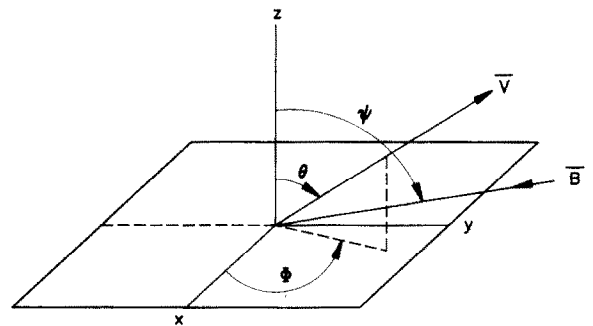


Fig. 1. Model geometry.

<sup>\*</sup> Work supported by the US Department of Energy, Office of Fusion Energy.

tial is modeled, based on considerations summarized in ref. [1] with the following dual structure:

$$\phi(z) = \phi_1 \exp(-z/2\lambda_D) + \phi_2 \exp(-z/R_{DT})$$

where  $\phi_1 + \phi_2 = \phi_0$  is the total sheath potential,  $\lambda_D$  is the Debye length at the start of the sheath, and  $R_{DT}$  is the D-T ion gyroradius. The electron density in the sheath is given as:

$$N_e = N_{e0} \exp(e\phi/kT_e).$$

The following parameters are used in the calculations;  $\psi = 87^\circ$ ,  $B = 5$  T,  $N_{e0} = 1 \times 10^{20}$  m<sup>3</sup>,  $e\phi_0/kT_e = -3$ . Values of  $\phi_1$  and  $\phi_2$  are used such that 25% of the total sheath potential difference occurs in the Debye sheath region  $0 \leq z \leq 6\lambda_D$ , and 75% occurs in the magnetic sheath,  $6\lambda_D \leq z \leq 3R_{DT}$ .

Impurity transport is treated by first computing the sputtering from an impinging current of D-T ions, and then following the resulting self-sputtering cascade arising from the redeposited impurities. For beryllium and carbon surfaces the FTRIM code was used to compute an array of sputtered atom launch velocities,  $\bar{V}$ , for 2000–10000 incident D-T ions, for  $T_e = 30, 75$  eV, and for a range of fractal dimensions  $D$ . The impinging D-T ion velocities were chosen from a distribution with monoenergetic energy of  $U_{DT} = 5 kT_e$ , a normal distribution in elevation angle with mean  $\theta_{DT} = 65^\circ$  and a standard deviation of  $10^\circ$ , and a fixed azimuthal angle of  $\Phi = 68^\circ$ . These values are based on typical calculated results for oblique incidence field geometries [4–6].

The atomic-scale fractal dimension of a surface can be measured by gas adsorption techniques. Surface roughness factors have been found this way [7] for fusion related materials. However, those experiments used just one size of adsorbed gas atom to make the measurements. By using a variety of adsorbate sizes a fractal dimension can be found. By using such a technique graphite has been shown to have fractal characteristics on the few to 100s Å scale ranging from a fractal dimension  $D$  of approximately 2.05 to 2.30 [8]. A range of  $D$  from 2.01 (very smooth surface) to 2.50 (very rough) was adopted for this work. (Values of  $D > 2.3$  are probably non-physical but are included to show trends.)

The D-T sputtering results are discussed in the following section. For tungsten, the D-T sputtering coefficient is too low to make the above procedure practical. Instead, a D-T sputtered array was generated assuming a constant  $W^0$  launch energy of  $U_0 = \frac{1}{2} U_B$ , for a binding energy  $U_B = 11.1$  eV, and using probability distribution functions  $f_1(\theta) = 2 \cos \theta \sin \theta$ , and  $f_2(\Phi) = 1/2\pi$ . This array for tungsten also simulates

sputtering by other low-Z plasma ions, notably, He<sup>+2</sup>.

To compute self-sputtering, a (variable) number of the impurity atoms from the D-T sputter array is launched. Transport of these particles in the plasma is followed by the WBC code [1]. The WBC code computes impurity transport due to charge changing and velocity changing collisions with the plasma; and the Lorentz force motion due to the electric and magnetic fields. If an impurity ion is redeposited, which almost all are in the regime studied, the particle velocity is used as input to FTRIM. The resulting reflected particle, if any, and any sputtered particles are then launched and followed by WBC. This procedure is iterated to follow a complete cascade from the D-T and self-sputtered atoms.

### 3. D-T sputtering results

Fig. 2 shows the calculated D-T sputtering coefficient for beryllium and carbon, for the conditions mentioned. For each case, 10000 flights were run for D-T on C, 2500 for D-T on Be at  $U_{DT} = 150$  eV ( $T_e = 30$  eV), and 2000 for D-T on Be at  $U_{DT} = 375$  eV ( $T_e = 75$  eV). Statistical errors are in the range of 3–5% for these cases.

As shown, increasing surface roughness decreases the D-T sputtering coefficient. It should be noted, however, that the yield for a case of  $D = 2.01$  is greater than that predicted for an atomically smooth surface with  $D = 2.00$  [3]. Although some degree of surface roughness allows primary knock-ons to become sputtered atoms directly without having to suffer any additional collisions, this is overcome by other potentially sputtered

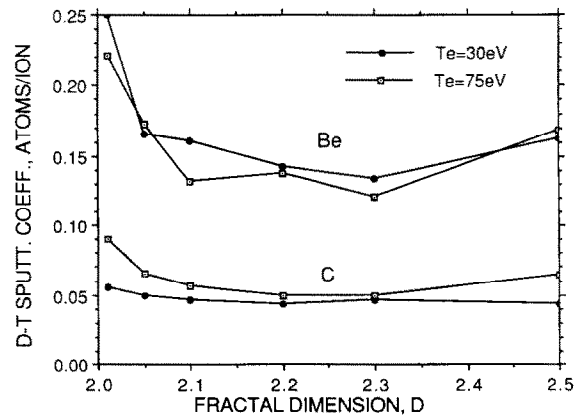


Fig. 2. D-T sputtering coefficients for beryllium and carbon as a function of fractal dimension.

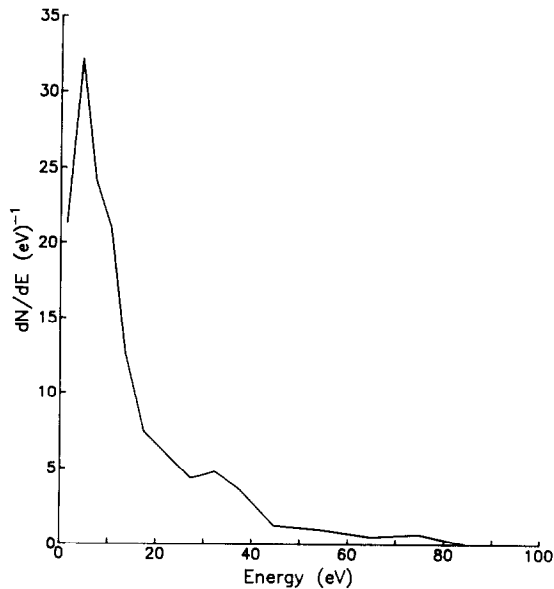


Fig. 3. Energy distribution of D-T sputtered carbon, for  $T_e = 30$  eV,  $D = 2.05$ ,  $U_{DT} = 150$  eV,  $\alpha = 65 \pm 10^\circ$ .

particles being captured by surface features as the surface roughness is increased.

A typical energy distribution of D-T sputtered particles is shown in fig. 3. The energy distribution is not a significant function of surface roughness. For most cases the angular distribution is also independent of surface roughness and is cosine in nature. However, for the

smallest incident/target mass ratio, i.e., D-T  $\rightarrow$  C an angular dependence on fractal dimension is evident. Figs. 4(a) and 4(b) show the elevation and azimuthal angular dependence respectively for the sputtered atoms at three degrees of surface roughness. For the smoothest case, the sputtered particles are peaked in the direction of the incident ion and come off at shallow elevation angles. As the roughness is increased the distribution becomes a cosine distribution and loses its azimuthal dependence.

#### 4. Self-sputtering results

Coupled computer code simulations were made as described above, to compute the D-T, and self-sputtering cascades. For each case a total of 600 sputtered particle histories were computed, with additional runs made to assess variances. (Because of differences in sputtering coefficients, each case involves a different mix of D-T sputtered and self-sputtered particles.) The non-vectorized coupled codes proved to be quite time consuming, with each particle history taking about 0.5 s CPU time on a CRAY2. We hope to speed this up in the future.

Table 1 lists values of some key impurity transport parameters, for a typical value of  $D = 2.1$ . In general, the average redeposited elevation angle, and charge

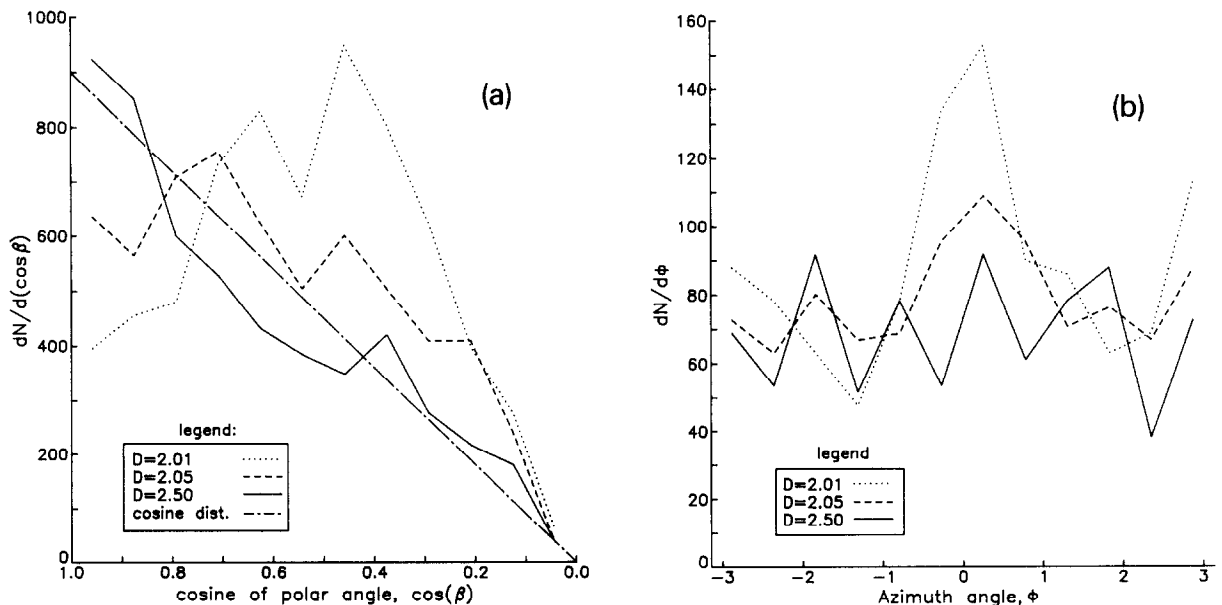


Fig. 4. (a,b). Angular distributions of D-T sputtered carbon, for  $T_e = 30$  eV;  $D = 2.01, 2.05, 2.5$ ;  $U_{DT} = 150$  eV;  $\alpha = 65 \pm 10^\circ$ .

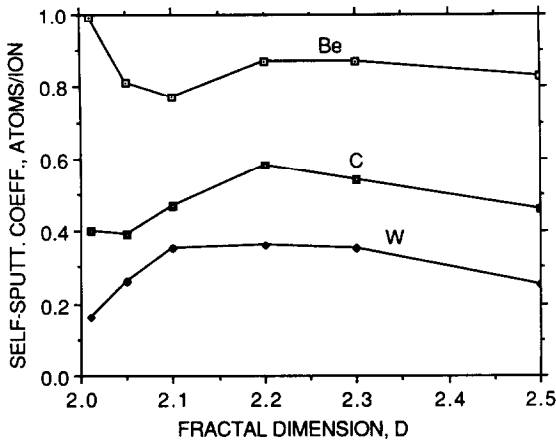


Fig. 5. Self-sputtering coefficients for beryllium, carbon, and tungsten, as a function of fractal dimension, for  $T_e = 30$  eV.

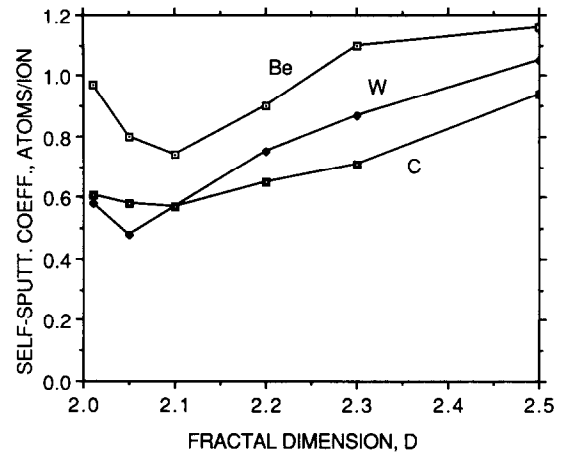


Fig. 6. Self-sputtering coefficients for beryllium, carbon, and tungsten as a function of fractal dimension, for  $T_e = 75$  eV.

state is fairly constant with  $D$ , while the average sputtered energy (not listed) and redeposited energy tend to increase somewhat with increasing roughness. As implied by the large variances in transit time there is a small but significant fraction of particles taking much longer than the average to be redeposited. This arises due to the impurity/plasma collision scaling properties. As was found in an earlier study [1] sputtered carbon, and in this case also beryllium, tend to be ionized outside of the sheath (approximate width  $3R_{DT} \approx 0.5$  mm, at  $T_e = 30$  eV) while tungsten, on average, is ionized within the sheath. The inclusion of D-T sputtered particle transport, in the present work, tends to lower the average charge state for tungsten, compared to

previous, self-sputtering only, results [1]. In general, redeposited charge states are all much lower than the coronal equilibrium values.

Figs. 5 and 6 show the average self-sputtering coefficient,  $\bar{Y}_{Z-Z'}$ , for the cases ran. This is defined as:  $\bar{Y}_{Z-Z'} = (\text{sputtered} + \text{reflected impurity atoms}) / (\text{incident impurity ions})$ . Statistical error in  $\bar{Y}_{Z-Z'}$  was found to be about 6% for the cases checked. For both values of  $T_e$  there is a minimum in self-sputtering coefficient, at low values of fractal dimension. Unlike light-atom sputtering, a great deal of energy can be transferred in a self-sputtering collision. If one of these higher energy sputtered particles strikes additional surface features on its way out of the surface, additional sputtered atoms

Table 1  
Impurity transport parameters for  $D = 2.1$

Parameter <sup>a)</sup>		$T_e = 30$ eV			$T_e = 75$ eV		
		Be	C	W	Be	C	W
Neutral ionization distance (perpendicular to surface)	$\bar{Z}_0$	2.0 mm	2.3 mm	0.27 mm	1.7 mm	2.0 mm	0.33 mm
Transit time <sup>b)</sup>	$\bar{\tau}$	3.0 $\mu$ s	3.0 $\mu$ s	0.41 $\mu$ s	3.4 $\mu$ s	3.6 $\mu$ s	0.39 $\mu$ s
	$\tau_{SD}$	3.9 $\mu$ s	3.7 $\mu$ s	1.0 $\mu$ s	7.8 $\mu$ s	6.3 $\mu$ s	1.4 $\mu$ s
Elevation angle <sup>c)</sup>	$\bar{\theta}$	48°	48°	18°	40°	44°	15°
	$\theta_{SD}$	15°	14°	12°	17°	17°	12°
Charge state <sup>c)</sup>	$\bar{K}$	1.6	2.0	2.1	1.5	2.2	2.2
	$K_{SD}$	0.48	0.82	1.4	0.50	1.2	2.1
Energy <sup>c)</sup>	$\bar{U}$	188 eV	233 eV	184 eV	339 eV	564 eV	442 eV
	$U_{SD}$	91 eV	125 eV	211 eV	175 eV	386 eV	687 eV

<sup>a)</sup> Bar denotes average value, SD denotes standard deviation.

<sup>b)</sup> From first ionization until redeposition.

<sup>c)</sup> Of redeposited ions.

can be created. This effect increases the sputtering yield at intermediate degrees of surface roughness compared to the light atom sputtering results.

In general, beryllium exhibits a close-to-unity self-sputtering coefficient at both temperatures even for smooth surfaces. This is similar to computational results found by Roth [9] using an a priori specification of oblique incidence impinging beryllium ion velocities. Carbon and tungsten appear substantially better at  $T_e = 30$  eV, and at  $T_e = 75$  eV as well, except for high and probably non-physical values of surface roughness,  $D = 2.5$ .

## 5. Conclusions

This work has examined surface roughness effects on sputtering and impurity transport for a divertor regime with 30–75 eV plasma temperatures at the sheath. The coupled computer codes used provide a self-consistent calculation of sputtering via the exchange of information about sputtered/redeposited particle velocities. The results indicate that surface roughness can play a significant role in determining erosion rates. A small degree of roughness, for example, decreases the computed D–T sputtering coefficient for carbon by  $\sim 40\%$ , for  $T_e = 75$  eV. Self-sputtering coefficients also can vary substantially with roughness, this is particularly important for values near unity.

Transport statistics of the combined D–T and self-sputtered impurity cascade were computed for the beryllium, carbon, and tungsten simulations. As seen in several previous studies, the low- $Z$  materials exhibit off-normal redeposited incidence ( $\bar{\theta} \approx 40\text{--}50^\circ$ ) whereas tungsten tends to impact at more normal incidence. Sputtered carbon and beryllium tend to be ionized outside of the sheath and depend, for the most part, on plasma collisions to be redeposited, whereas tungsten tends to be redeposited much faster due to sheath electric field acceleration.

In general the sputtering results for beryllium appear discouraging, with high D–T and self-sputtering coefficients predicted at all values of fractal dimension  $D$ .

There is, however, a roughness regime ( $D \approx 2.1$ ) where beryllium sputtering would be minimized. Carbon appears to offer much better sputtering erosion performance than beryllium. The present results for tungsten are encouraging, implying stable ( $\bar{Y}_{Z \rightarrow Z} < 1$ ) operation for  $T_e = 75$  eV, for physically plausible values of surface roughness. This supports earlier results [1] which used a simpler sputtering-model (but examined the plasma operating regime in much more detail).

These conclusions are subject to numerous uncertainties in the models used, e.g., in plasma collision terms, sheath structure, and limitations in the binary collision methodology of the TRIM code. Experimental data needed for code verification is, for the most part, lacking. Experiments to measure surface roughness are possible, and would appear to be desirable, in view of the trends shown here.

## Acknowledgements

We would like to thank the Max-Planck-Institut für Plasmaphysik for permission to use the TRIM code, and the National Center for Supercomputing Applications at the University of Illinois for computational support.

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